

SECOND LEVEL ANALYSIS OF FMRI

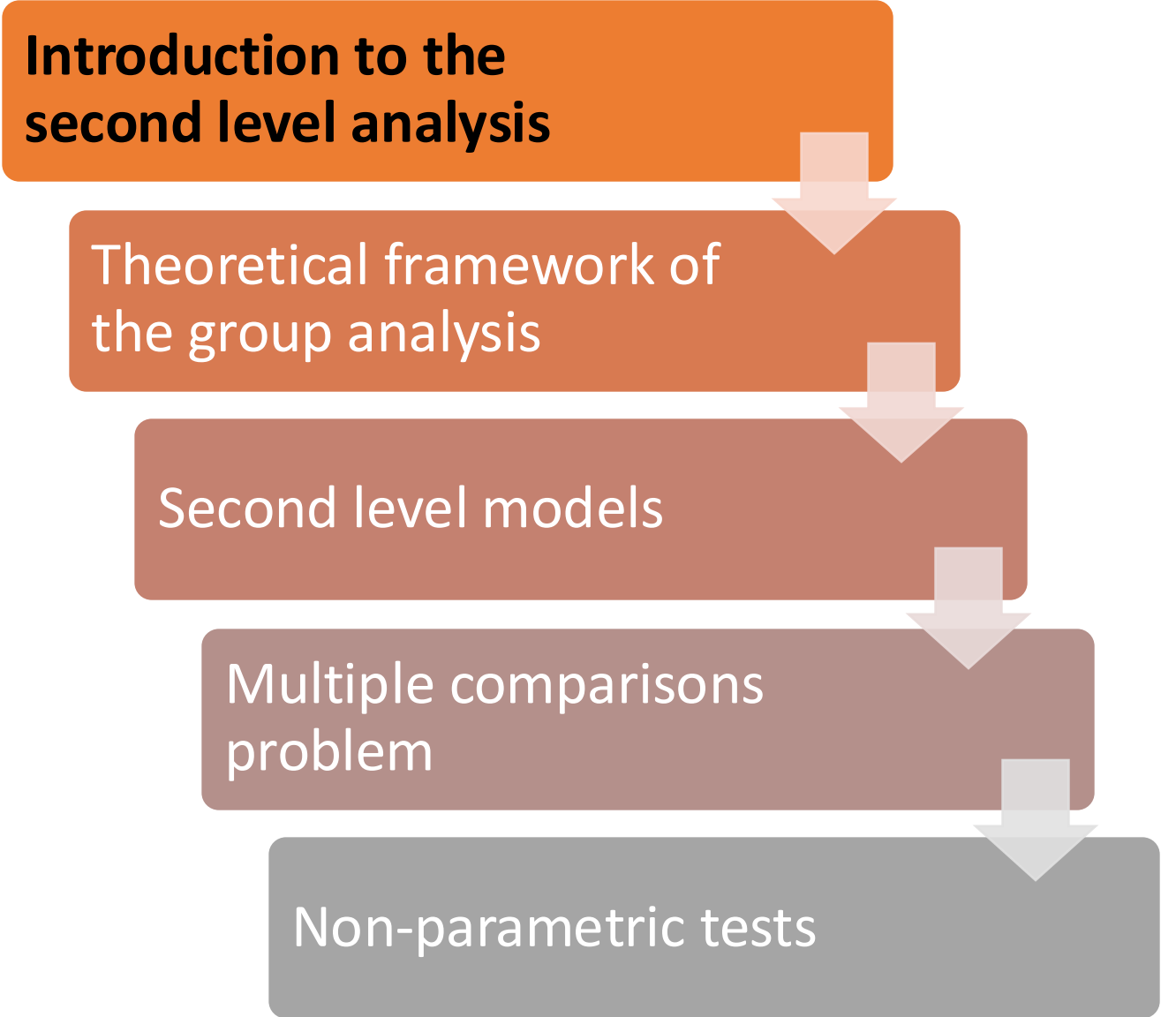
Turku PET Centre Brain Imaging Course 2025

Severi Santavirta, Turku PET Centre



Topics

**Introduction to the
second level analysis**



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graph TD; A[Introduction to the second level analysis] --> B[Theoretical framework of the group analysis]; B --> C[Second level models]; C --> D[Multiple comparisons problem]; D --> E[Non-parametric tests];
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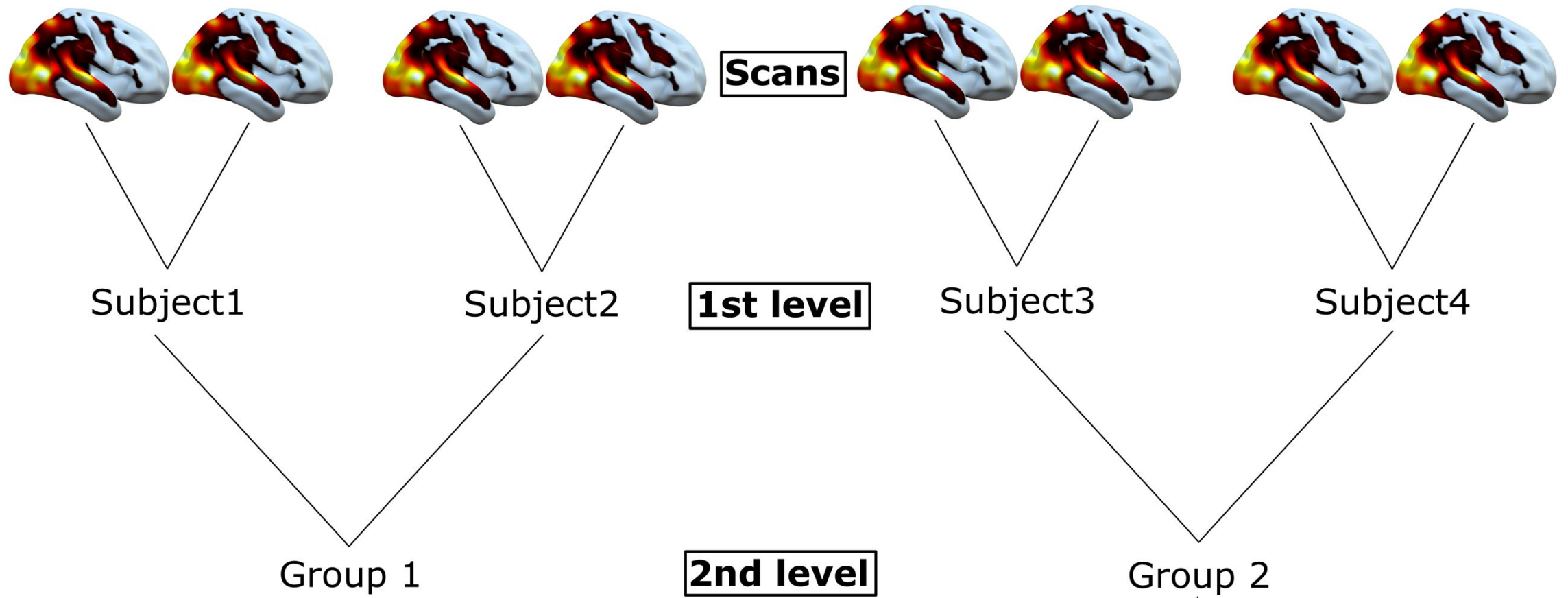
Theoretical framework of
the group analysis

Second level models

Multiple comparisons
problem

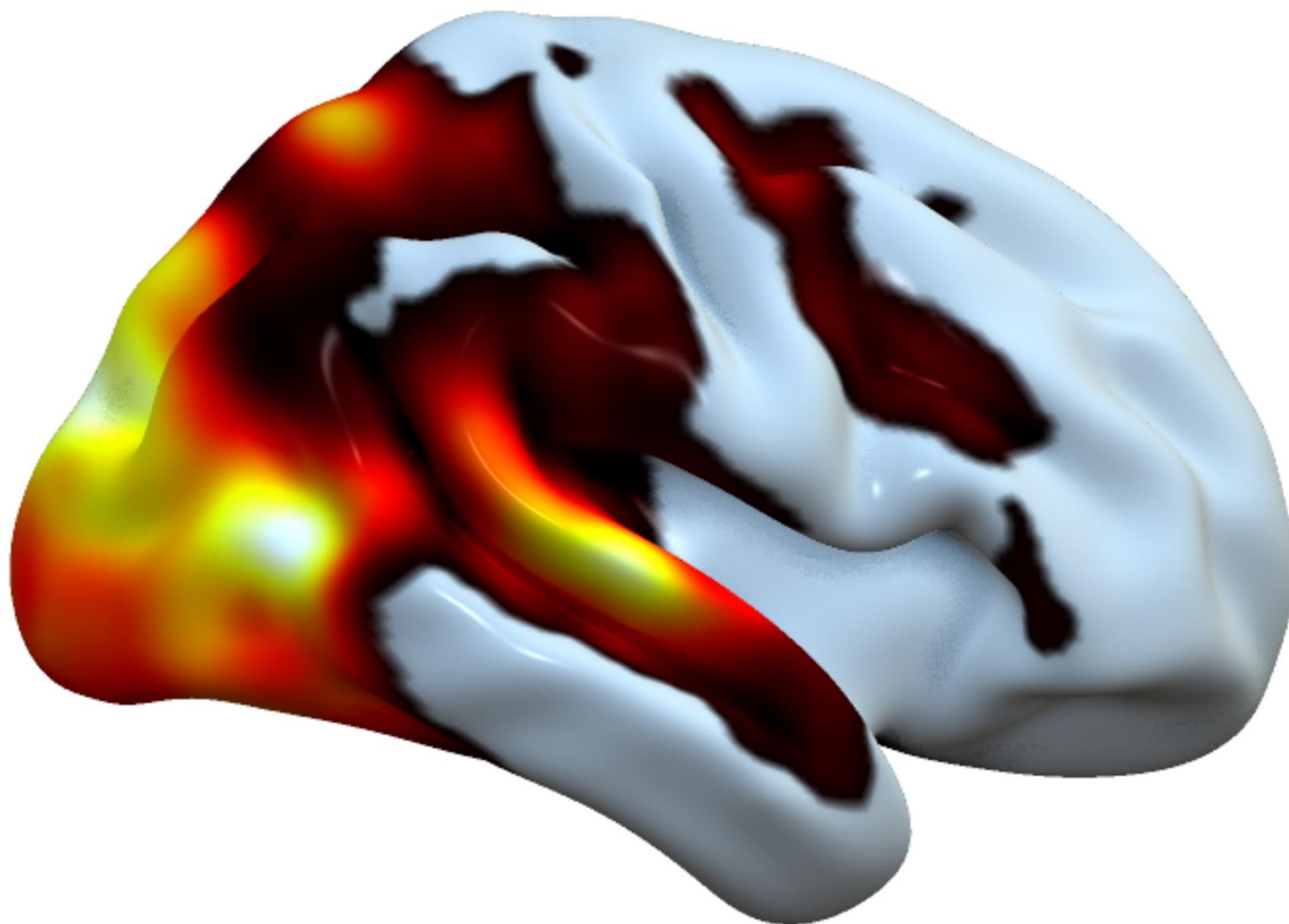
Non-parametric tests

Hierarchical data



Whole brain analysis
 Voxel-level analysis
 Massive univariate analysis

➡ The same thing!



Region-of-interest (ROI) analysis

Temporal lobe	Temporal Pole Superior	*
	Heschl	*
	Temporal Superior	*
	Temporal Middle	*
Occipital lobe	Occipital Inferior	*
	Occipital Middle	*
	Occipital Superior	*
	Lingual	*
	Calcarine	*
	Cuneus	*
	Fusiform	*
Parietal lobe	Parietal Superior	*
	Parietal Inferior	*
	Supramarginal	*
	Rolandic Operculum	*
	Precuneus	*
	Angular	*
	Paracentral Lobule	*
	Postcentral	*
	Precentral	*
Frontal lobe	Supplementary Motor Area	*
	Cingulate Posterior	*
	Cingulate Middle	*
	Cingulate Anterior	*
	Frontal Superior	*
	Frontal Superior Medial	*
	Frontal Middle	*
	Frontal Inferior Triangular	*
	Frontal Inferior Operculum	*
	Frontal Inferior Orbital	*
	Orbitofrontal Posterior	*
	Orbitofrontal Lateral	*
	Olfactory	*
	Parahippocampal	*
Subcortex	Hippocampus	*
	Insula	*
	Amygdala	*
	Thalamus	*
	Pallidum	*
	Caudate	*
	Putamen	*

The data between subjects should be comparable



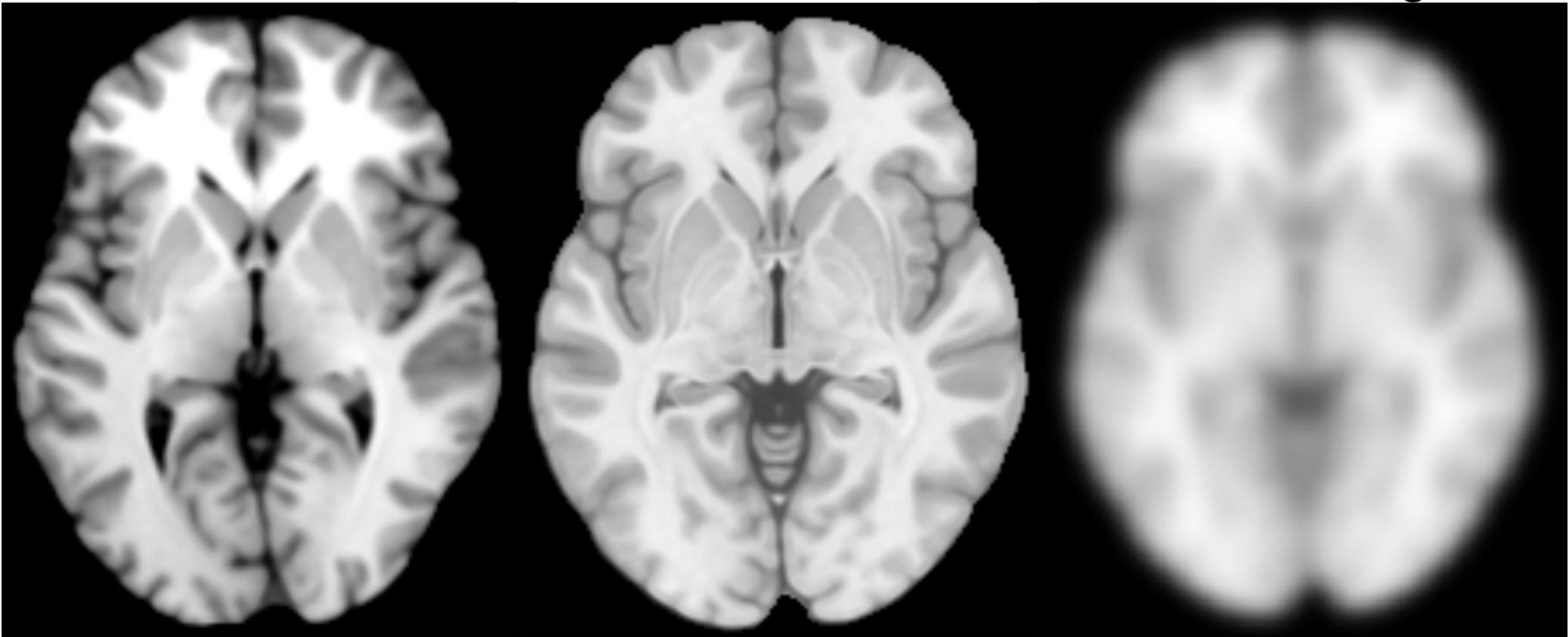
Preprocess data before analysis



Motion correction

Normalization

Smoothing



What if I am only interested in doing ROI analysis?

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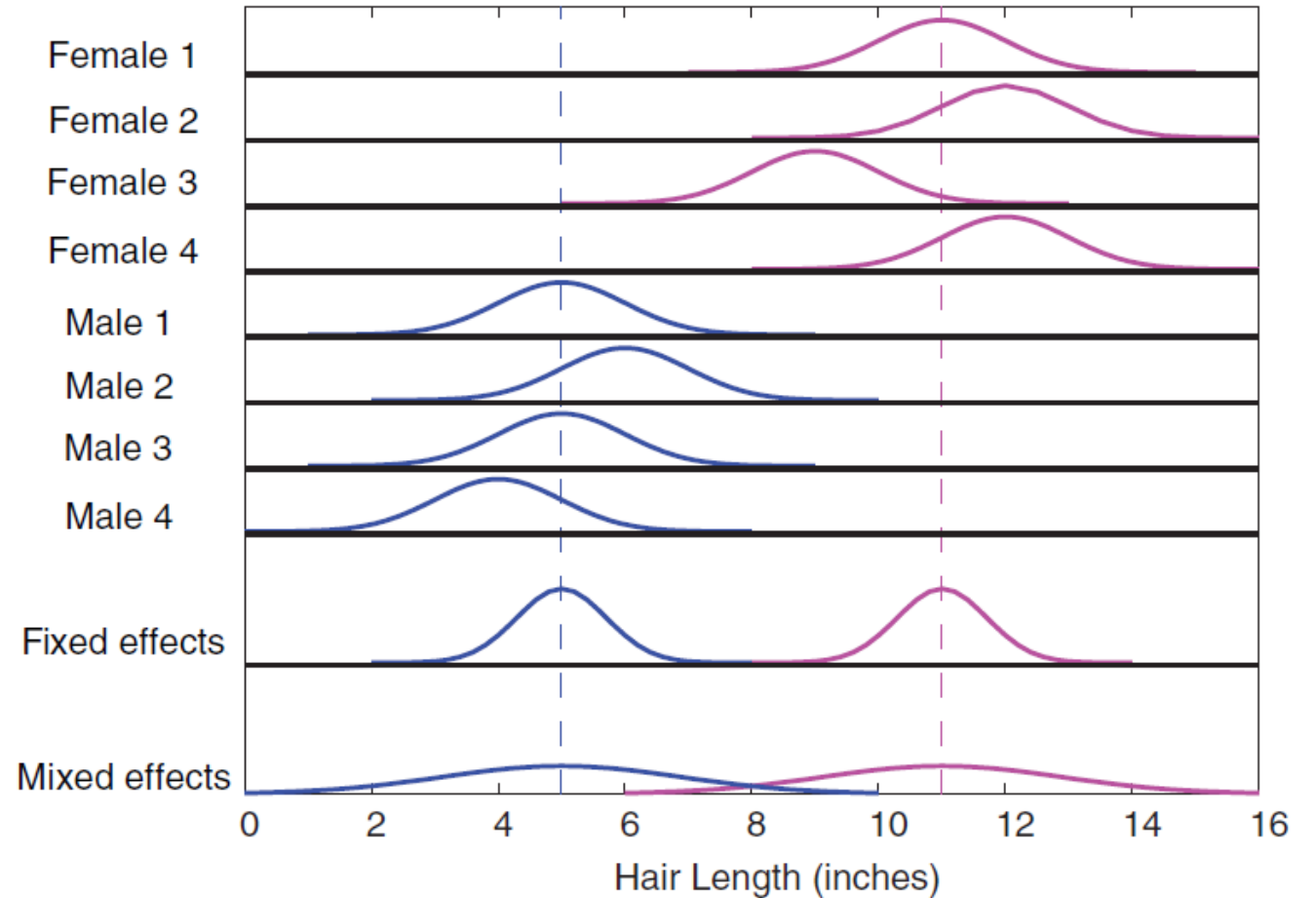
Non-parametric tests

1st level analysis, 2nd level analysis, fixed effects, mixed effects... HELP!

Basic sources of variation in fMRI (or hair length)

Var^W = within-subject variance

Var^B = between-subject variance



(Poldrack, Nichols, & Mumford, 2011)

Fixed effects model

$$\text{Var}^W$$

Describe study sample only

Combine repeated measures
within subjects

Variance
used in the analysis

Results

Application

Mixed effects model

$$\text{Var}^W + \text{Var}^B$$

Generalize to population

Group analysis of fMRI

Mixed effects model in fMRI mathematically

- Within subject variance estimation (1st level model)

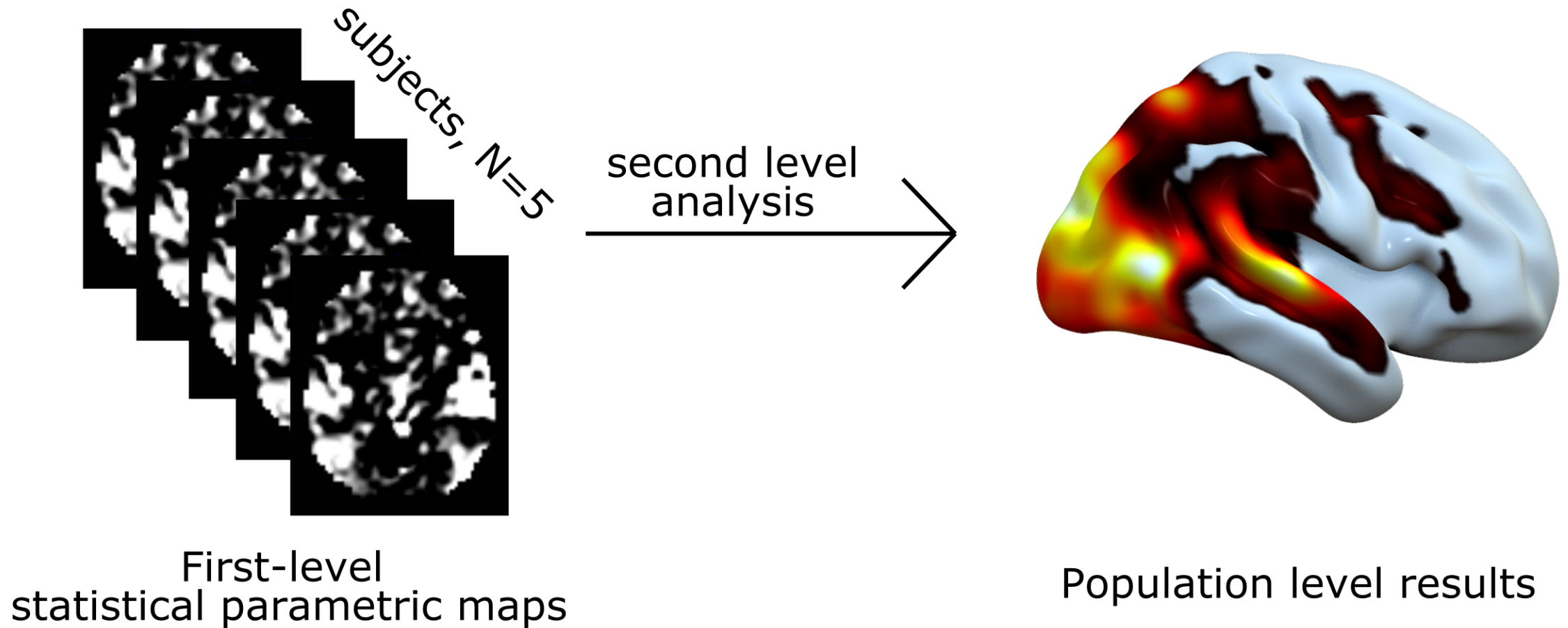
$$Y_s = \beta_s X + \varepsilon_s, \varepsilon_s \sim N(0, \sigma_{subject}^2) \quad (1)$$

- Between subject variance estimation (2nd level model)

$$\beta_s = \beta_b X_b + \varepsilon_b, \varepsilon_b \sim N(0, \sigma_{between}^2) \quad (2)$$

- Full mixed effects model would estimate within & between subject variances simultaneously => Computationally demanding to estimate!

Summary statistics approach (mixed effect model)



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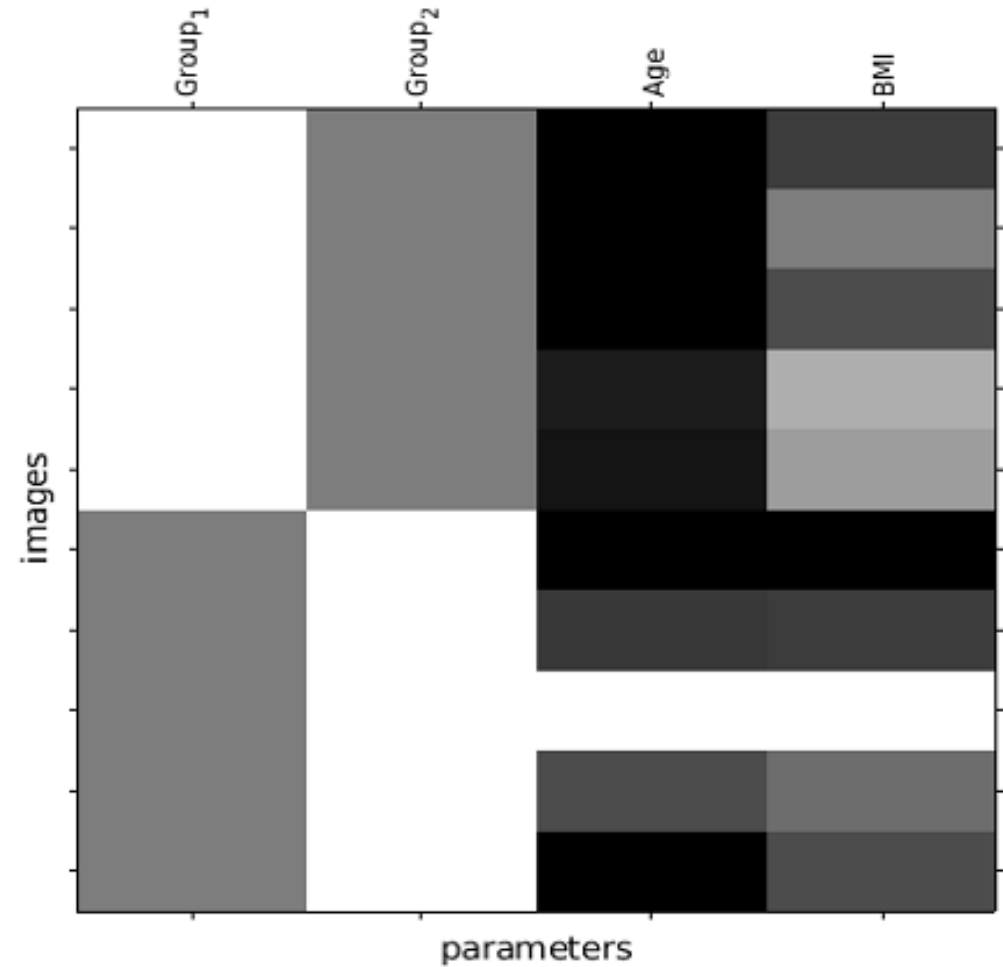
Multiple comparisons
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Non-parametric tests

Second level design matrix in SPM

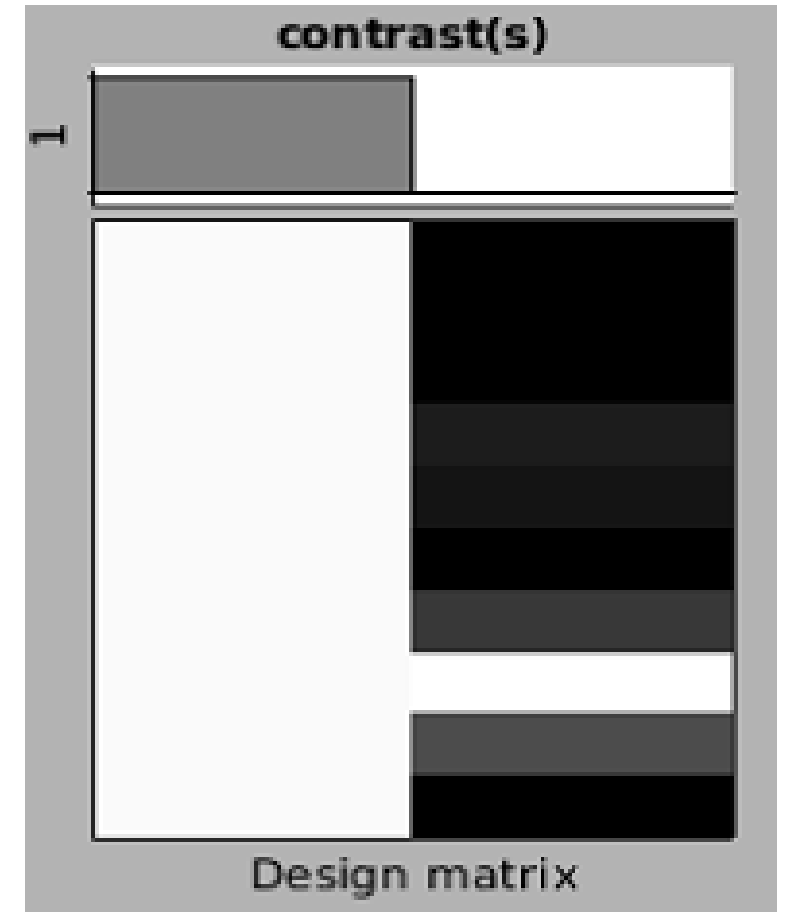
- Rows
 - Subjects
- Columns
 - Variables describing between subject variatio
 - Effect of each column will be estimated



One sample T-test

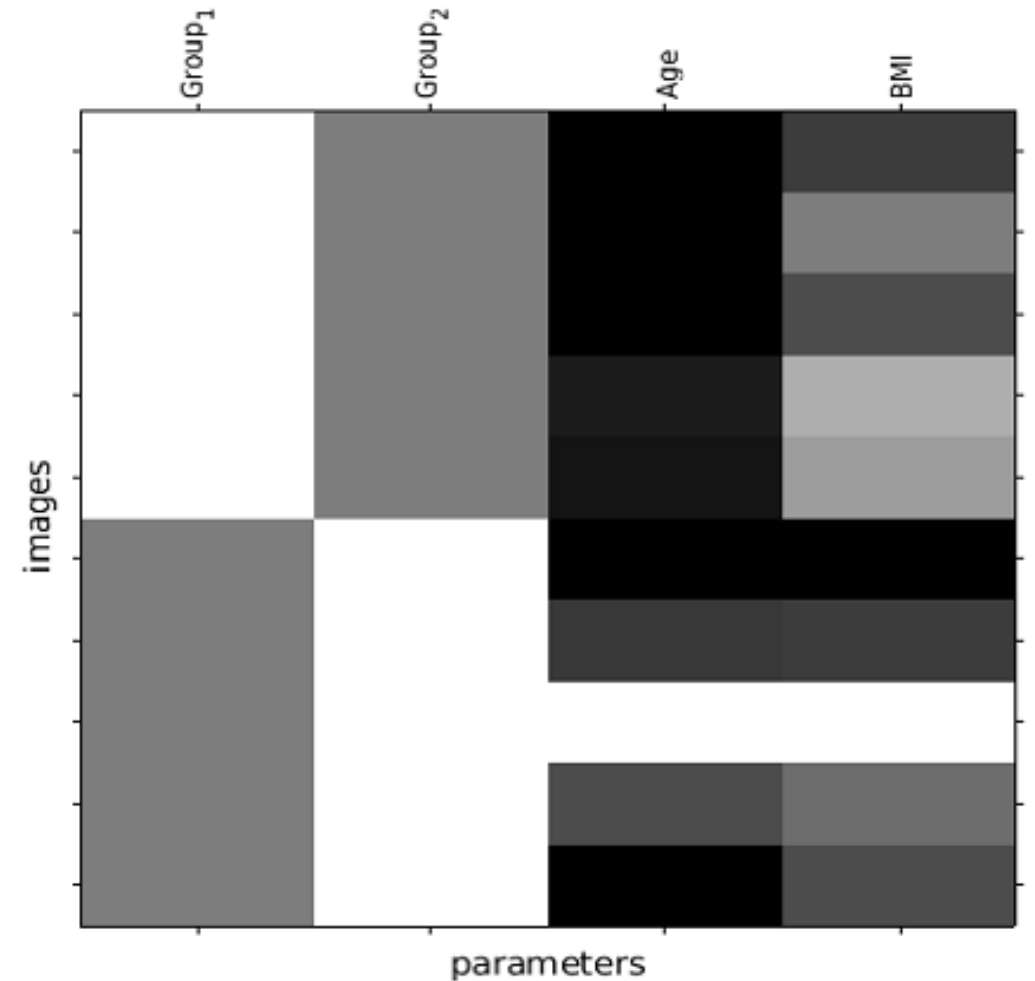
$$\beta_{1st\ level} = \beta_{main} + \beta_{2nd\ level} X_{covariate}$$

- $\beta_{1st\ level}$
 - Subjectwise association between the stimulus condition and BOLD signal
 - These are estimated in the 1st level analysis
- β_{main}
 - Is BOLD signal associated with the stimulus condition on the population level?
 - [1 0] in SPM contrast manager
- $\beta_{2nd\ level}$
 - Does a subjective factor (e.g age) explain the subjectwise differences in the association?
 - [0 1] in SPM contrast manager for positive effect
 - [0 -1] for negative effect



Two sample T-test

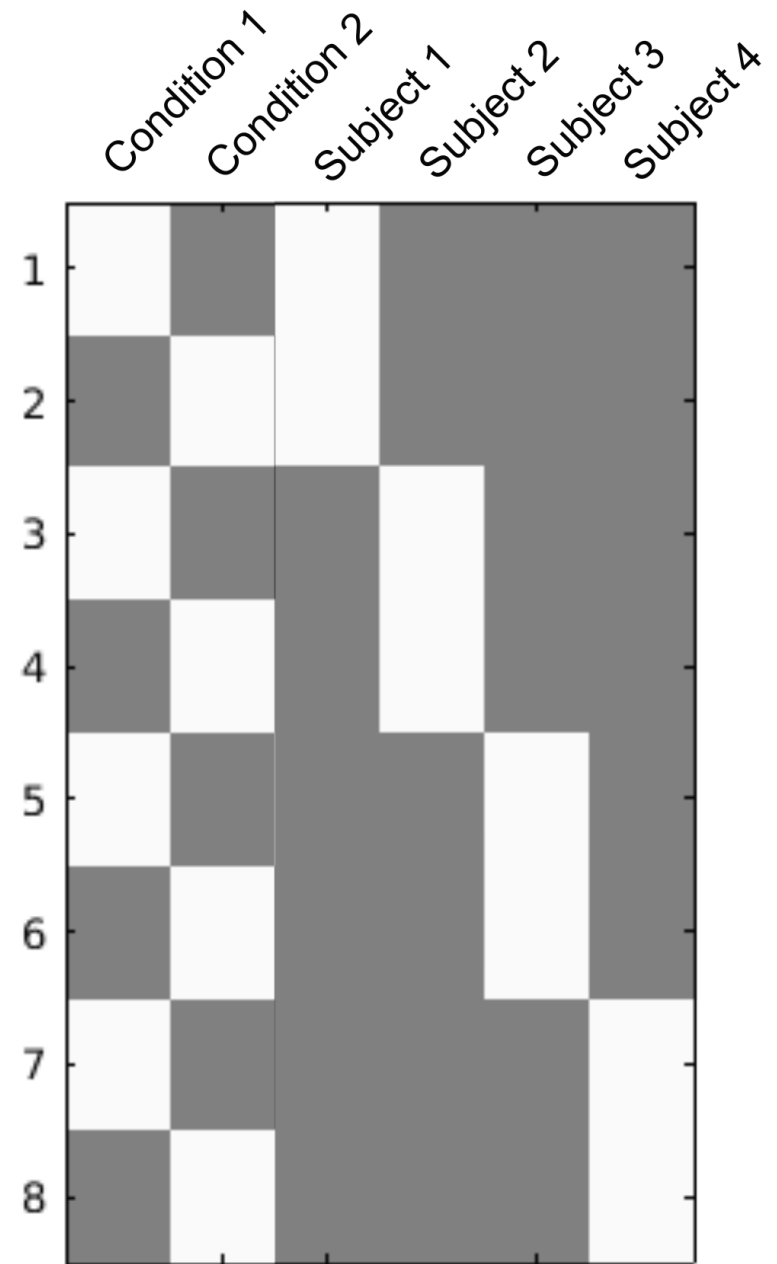
- H: Brain activity is different between two groups of subjects
- Group1 > Group2 with two additional covariates
 - SPM contrast $[1 \ -1 \ 0 \ 0] = \beta_{gr1} - \beta_{gr2}$
 - “Whether females have increased brain response for the 1st level condition than males when age and BMI are controlled for”



$$\beta_{\text{contrast}} = \beta_{gr1}X_{gr1} + \beta_{gr2}X_{gr2} + \beta_{age}X_{age} + \beta_{bmi}X_{bmi}$$

Paired T-test

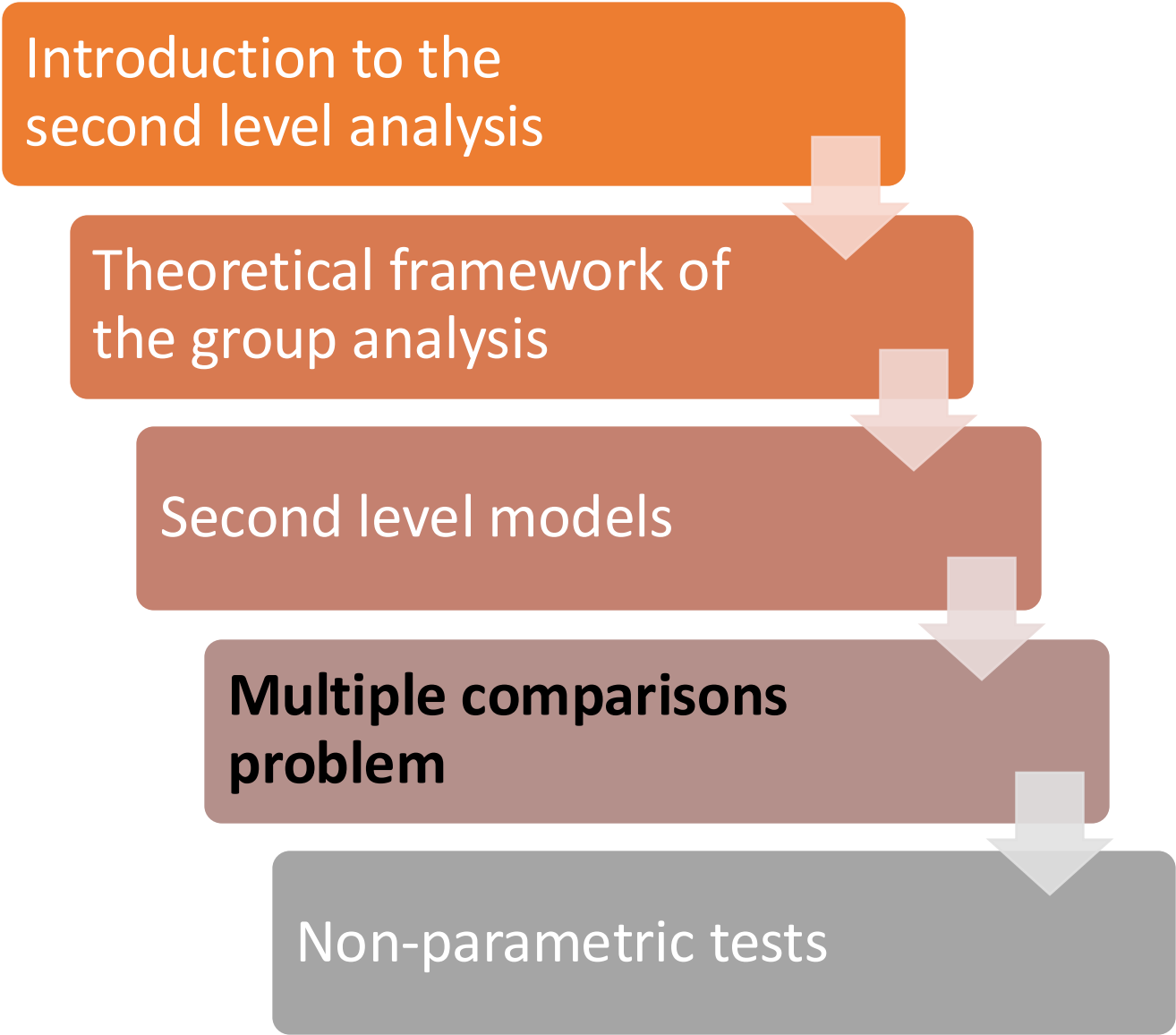
- H: There is a difference between conditions in the brain response (two scans per subject)
- 4 subjects, 2 scans per subject
- Condition
 - Cross-sectional
 - Baseline vs. Stimulus
 - Longitudinal
 - Before treatment vs. After treatment
- Condition 2 > Condition 1
 - SPM contrast $[-1 \ 1 \ 0 \ 0 \ 0 \ 0] = -\beta_{c1} + \beta_{c2}$
 - "Brain response associated with happy faces is higher after treatment"



$$\beta_{\text{contrast}} = \beta_{c1}X_{c1} + \beta_{c2}X_{c2} + \beta_{s1}X_{s1} + \beta_{s2}X_{s2} + \beta_{s2}X_{s2} + \beta_{s2}X_{s2}$$

Topics

Introduction to the
second level analysis



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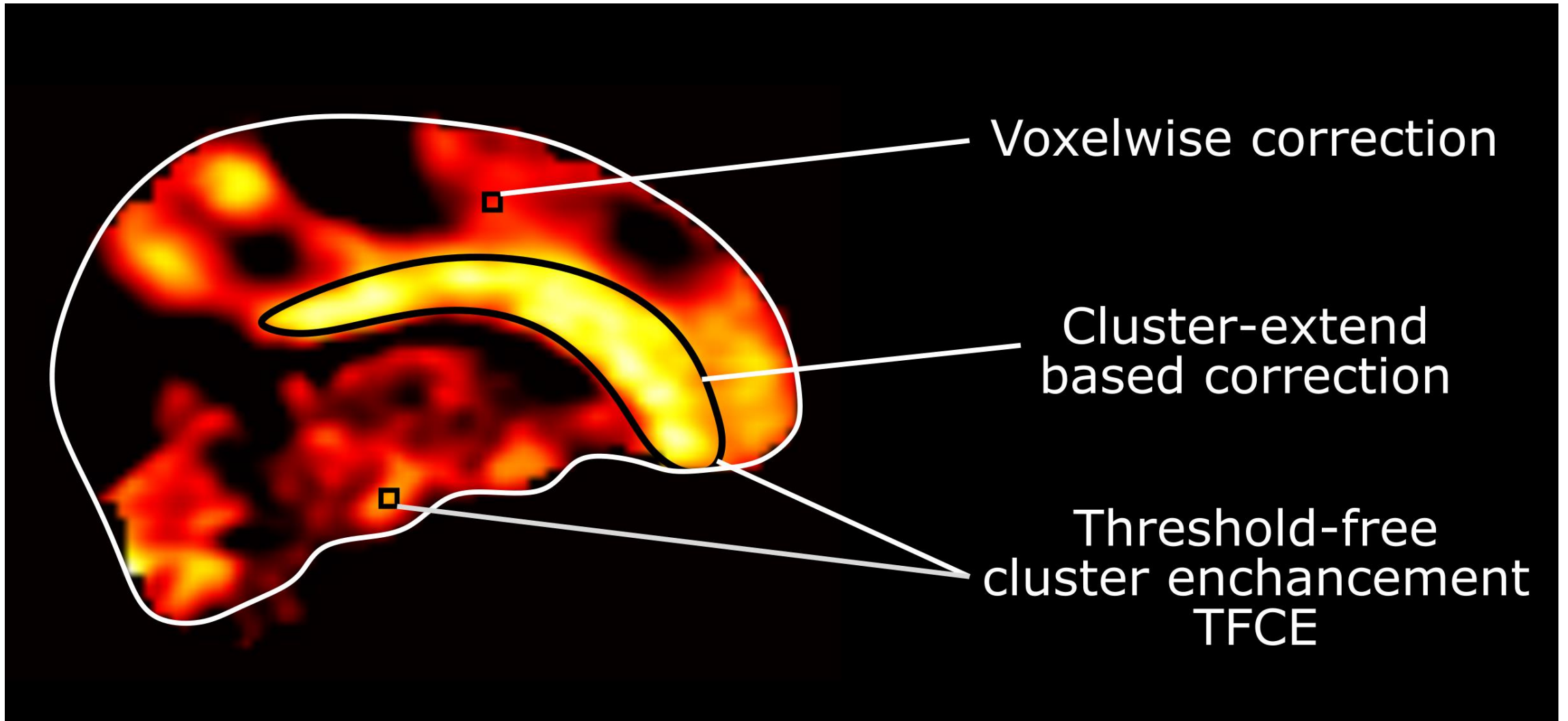
Theoretical framework of
the group analysis

Second level models

**Multiple comparisons
problem**

Non-parametric tests

Multiple comparisons correction methods



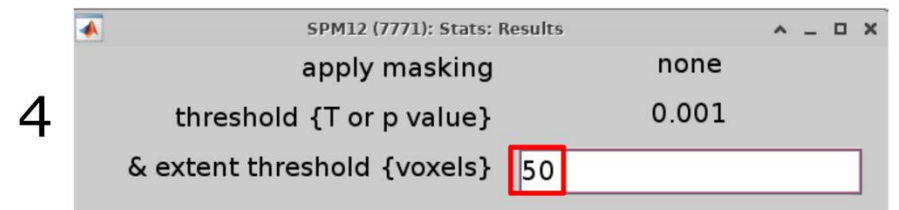
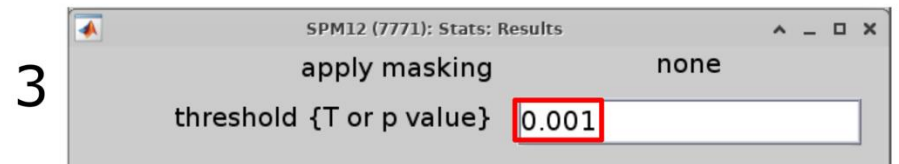
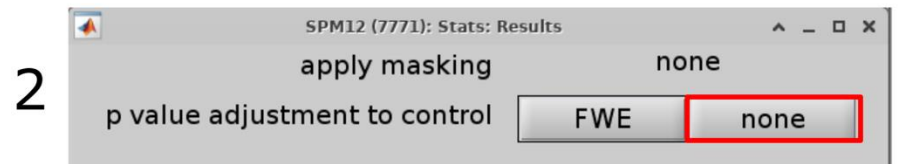
(Review: Lindquist & Mejia, 2015)

Voxelwise multiple comparisons correction

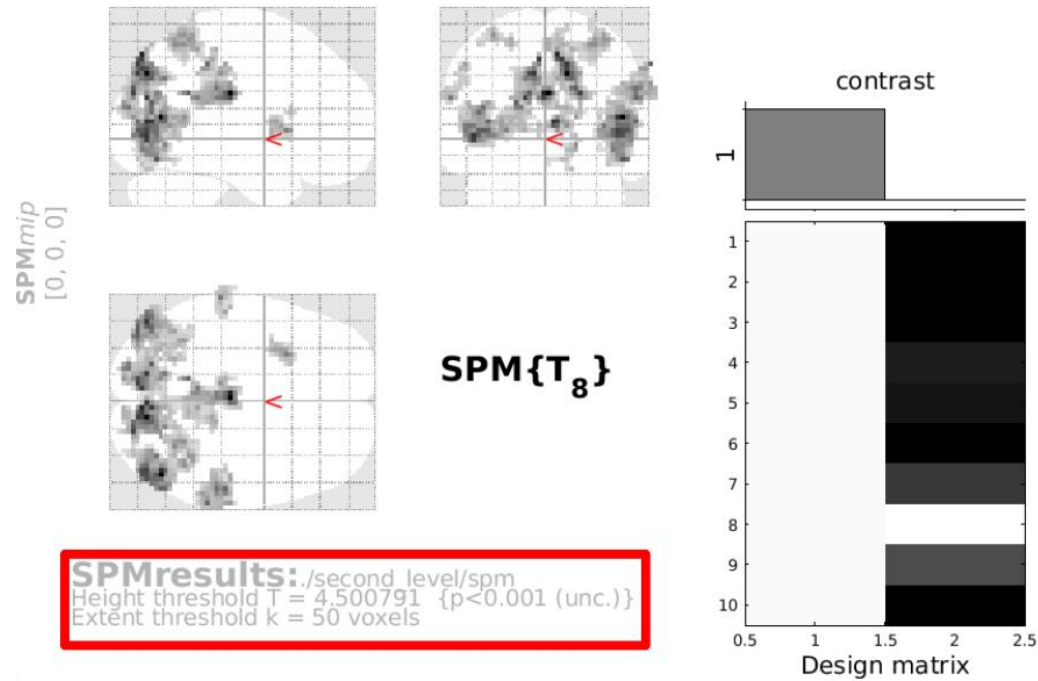
- Family-wise error rate (FWER) (Lindquist & Mejia, 2015)
 - Probability of making one or more false positives
 - Bonferroni correction
 - “5% probability that there is **at least one** false positive finding”
 - $0.05 / \text{number of tests} = \text{corrected p-value threshold}$
- False discovery rate (Benjamini & Hochberg, 1995)
 - “On average **no more than 5%** of our findings are false positives”

Cluster-extend based correction (Lindquist & Mejia, 2015)

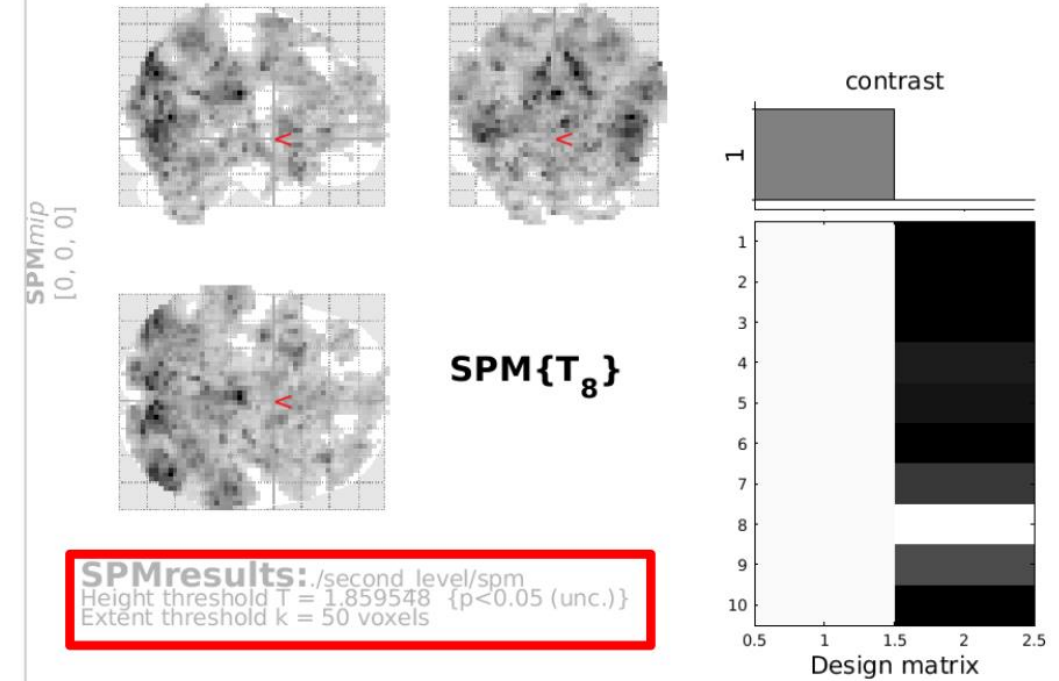
- Accounts for the spatial dependency between voxels
- “What is the probability to observe an activating cluster of this size under the null hypothesis of no activation”
- Two-step procedure
 1. Choose primary voxel-level threshold
 1. e.g. $p < 0.001$
 2. Choose minimum size of a cluster
 1. As number of voxels, e.g. 50
 2. Usually selected based on the desired cluster level FWER level
- Be cautious, may yield more false positives than expected



Main effect



Main effect



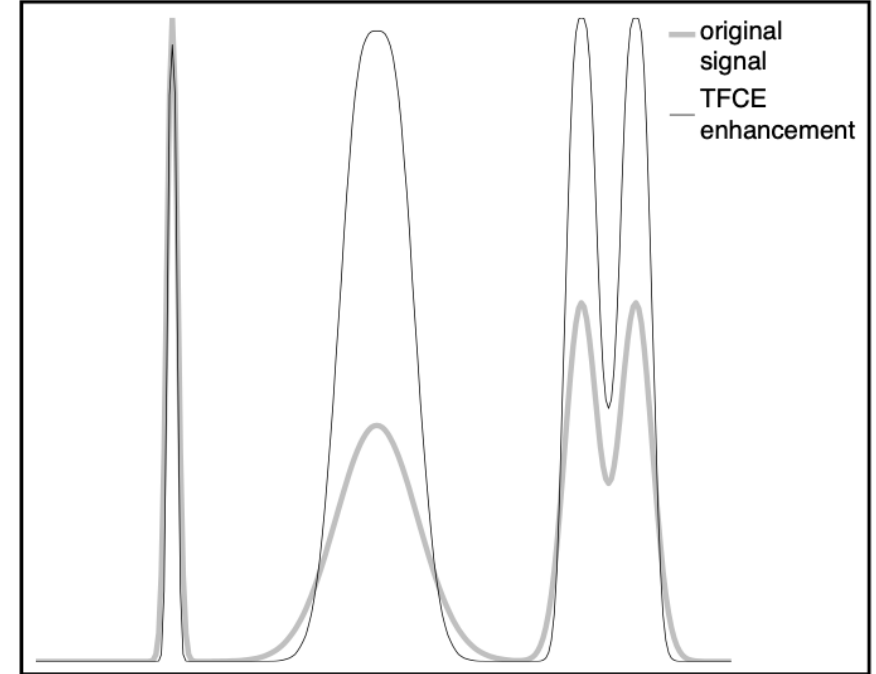
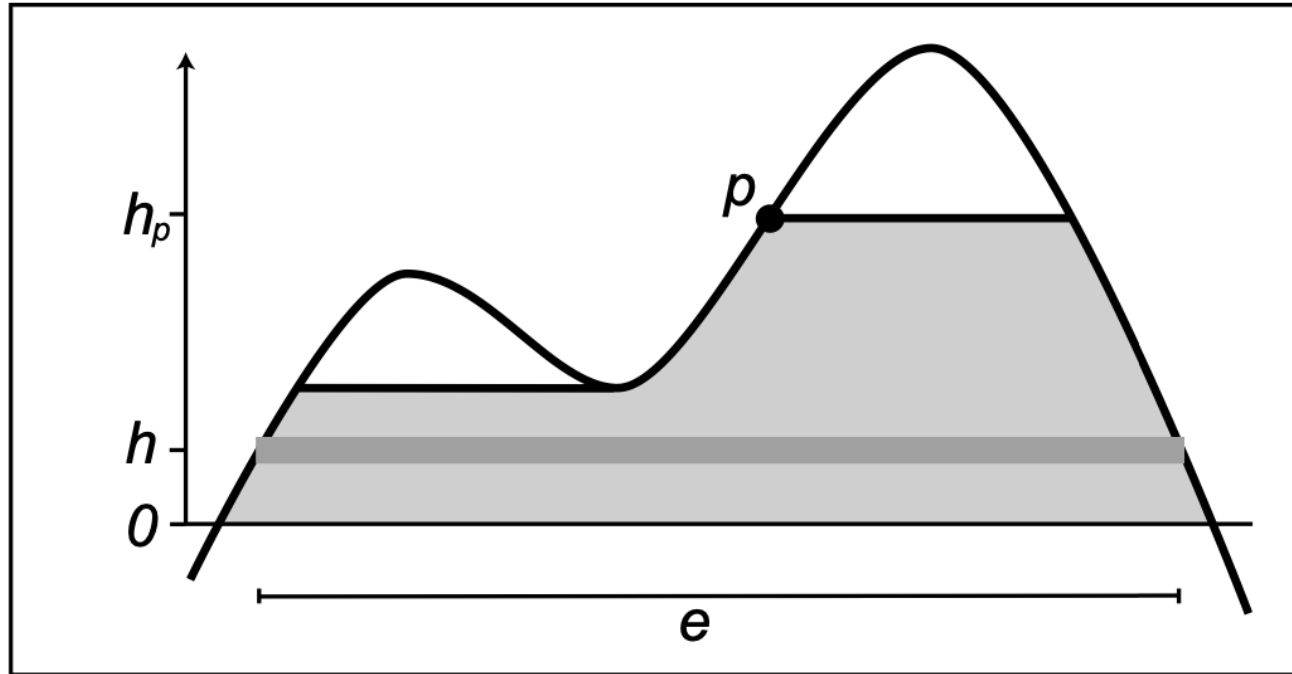
Statistics: p -values adjusted for search volume

set-level		cluster-level				peak-level					mm mm mm		
p	c	$p_{\text{FWE-corr}}$	$q_{\text{FDR-corr}}$	k_E	p_{uncorr}	$p_{\text{FWE-corr}}$	$q_{\text{FDR-corr}}$	T	(Z_E)	p_{uncorr}			
0.000	10	0.000	0.000	453	0.000	0.014	0.507	14.69	5.04	0.000	48	-69	12
						0.099	0.507	11.33	4.65	0.000	45	-78	3
						0.188	0.581	10.40	4.52	0.000	48	-72	-15
		0.000	0.000	166	0.000	0.016	0.507	14.39	5.01	0.000	0	-24	27
						0.242	0.581	10.06	4.46	0.000	-12	-51	27
						0.593	0.581	8.91	4.27	0.000	0	-33	24
		0.000	0.000	1011	0.000	0.019	0.507	14.10	4.98	0.000	12	-78	39
						0.040	0.507	12.77	4.83	0.000	6	-81	51
						0.061	0.507	12.06	4.75	0.000	3	-78	9
		0.000	0.000	202	0.000	0.296	0.581	9.79	4.42	0.000	66	-39	45
						0.296	0.581	9.79	4.42	0.000	57	-27	24
						0.425	0.581	9.32	4.34	0.000	57	-33	30
		0.000	0.000	57	0.000	0.536	0.581	9.03	4.29	0.000	-63	-30	24
						0.999	0.606	7.34	3.94	0.000	-54	-27	45
						1.000	0.824	5.45	3.43	0.000	-57	-33	33
		0.000	0.000	68	0.000	0.764	0.581	8.61	4.21	0.000	-27	12	3
						1.000	0.641	6.70	3.79	0.000	-30	3	3
						1.000	0.719	6.05	3.61	0.000	-21	15	15
		0.000	0.000	55	0.000	0.831	0.591	8.51	4.19	0.000	18	-66	-6
						1.000	0.694	6.24	3.66	0.000	18	-60	0
						1.000	0.705	6.20	3.65	0.000	12	-72	-9
		0.000	0.000	130	0.000	0.991	0.606	8.17	4.12	0.000	30	-60	57

Statistics: p -values adjusted for search volume

set-level		cluster-level				peak-level					mm mm mm		
p	c	$p_{\text{FWE-corr}}$	$q_{\text{FDR-corr}}$	k_E	p_{uncorr}	$p_{\text{FWE-corr}}$	$q_{\text{FDR-corr}}$	T	(Z_E)	p_{uncorr}			
1.000	3	0.000	0.000	18190	0.000	0.014	0.309	14.69	5.04	0.000	48	-69	12
						0.016	0.309	14.39	5.01	0.000	0	-24	27
						0.019	0.309	14.10	4.98	0.000	12	-78	39
		0.003	0.000	668	0.000	0.536	0.355	9.03	4.29	0.000	-63	-30	24
						0.999	0.370	7.34	3.94	0.000	-54	-27	45
						1.000	0.503	5.45	3.43	0.000	-57	-33	33
		0.893	0.253	163	0.013	1.000	0.490	5.60	3.48	0.000	-36	39	24
						1.000	0.503	5.34	3.39	0.000	-39	45	33
						1.000	0.658	4.22	2.98	0.001	-24	42	33

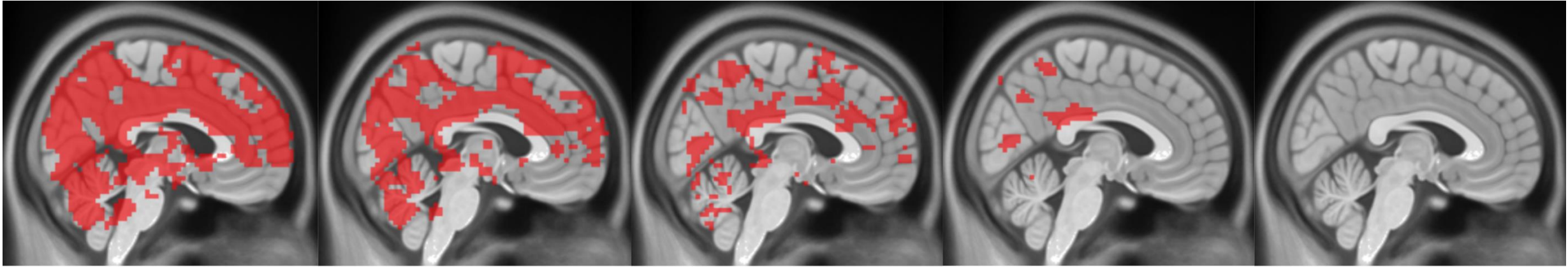
Threshold-free cluster enhancement (TFCE)



TFCE = h_p (voxelwise t-value) * e (amount of supporting voxels)

→ The voxelwise significance is adjusted by the amount supporting voxels

→ Significance of each voxel is assessed with permutations and then corrected for multiple comparisons



TFCE
(randomise)

Cluster FWE
 $p < 0.05, k = 50$

FDR $\alpha = 0.05$
(randomise)

Cluster FWE
 $p < 0.001, k = 50$

Bonferroni/FWE
 $p < 0.05$

False positives

False negatives

Conservative correction inflates effect size estimates

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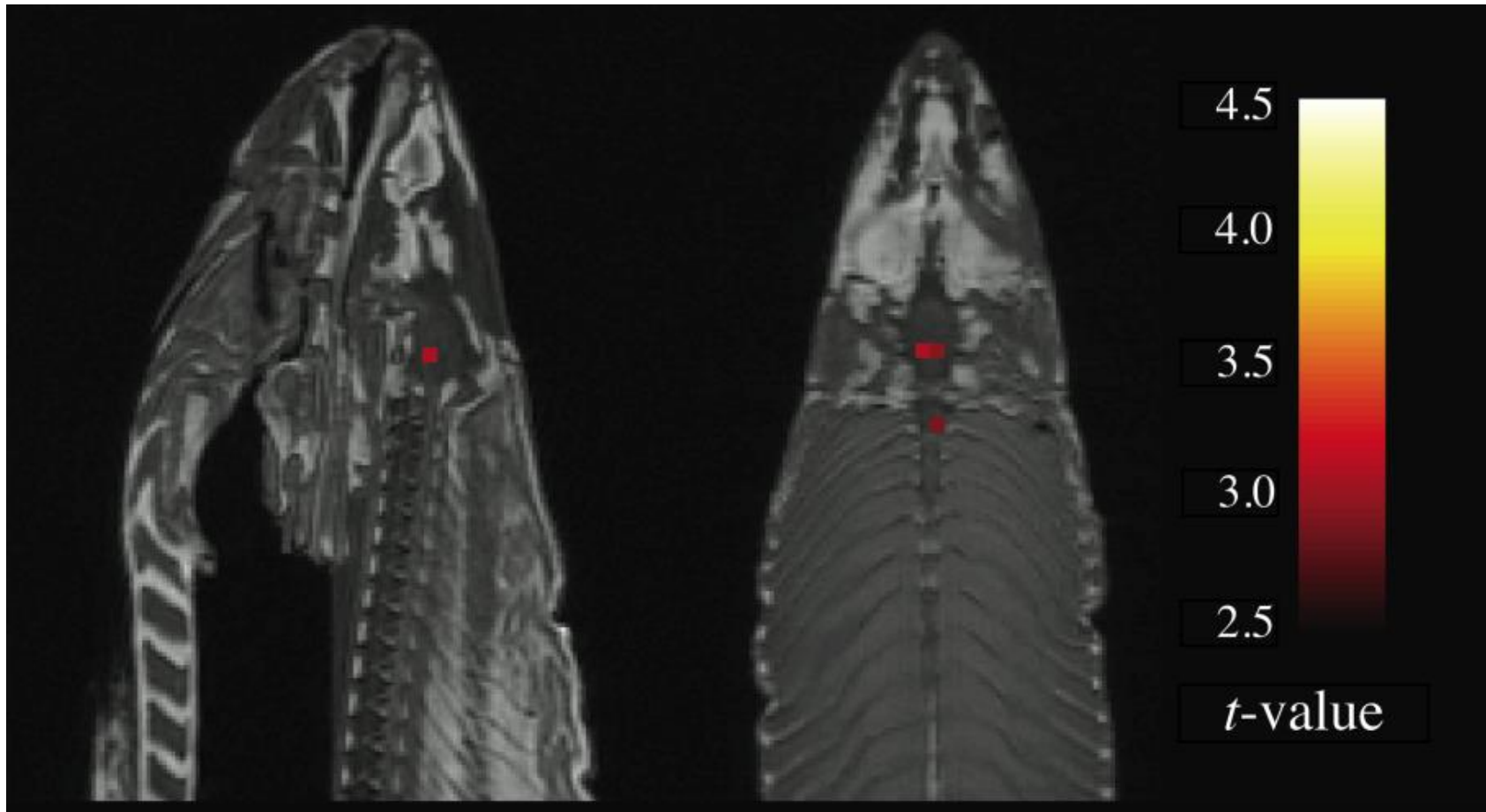
Non-parametric tests

Non-parametric tests

- Motivation for non-parametric tests in group analyses (Eklund, Nichols, & Knutsson, 2016)
 1. Voxelwise multiple comparisons methods may produce too conservative findings and cluster-based methods more false positives than expected
 2. Non-parametric tests have been shown to correct better for multiple comparisons.
 3. Non-parametric tests do not make assumptions of the distribution of the statistic.
- Tools for non-parametric tests
 - SnPM (Doc: <https://warwick.ac.uk/fac/sci/statistics/staff/academic-research/nichols/software/snpm>)
 - FSL Randomise (Winkler, Ridgway, Webster, Smith & Nichols, 2014)
 - One and two sample (unpaired/paired) T-tests, repeated measures anova
 - Easy to output statistical result maps with various different multiple comparisons methods
 - Including TFCE method
 - Doc: <https://fsl.fmrib.ox.ac.uk/fsl/fslwiki/Randomise>

Do not end up finding activations in a dead salmon's brain.

Correct for multiple comparisons!



Computer demonstrations

- horizon.utu.fi
 - Virtual desktop: **Ubuntu Mate 22.04 PSYK8965**
 - Only registered students with **utu accounts** can access.
 - Make sure that you have **unix permissions** set up well before the classes!
 - idm.utu.fi -> My information -> Add UNIX access

References

- Benjamini, Y., & Hochberg, Y. (1995). Controlling the False Discovery Rate - a Practical and Powerful Approach to Multiple Testing. *Journal of the Royal Statistical Society Series B-Statistical Methodology*, 57(1), 289-300. doi:DOI 10.1111/j.2517-6161.1995.tb02031.x
- Eklund, A., Nichols, T. E., & Knutsson, H. (2016). Cluster failure: Why fMRI inferences for spatial extent have inflated false-positive rates. *Proc Natl Acad Sci U S A*, 113(28), 7900-7905. doi:10.1073/pnas.1602413113
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