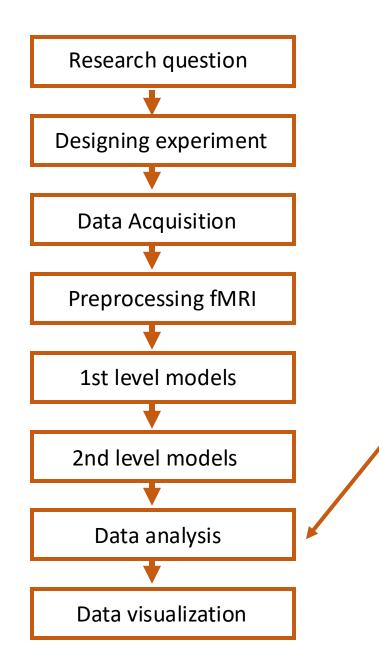
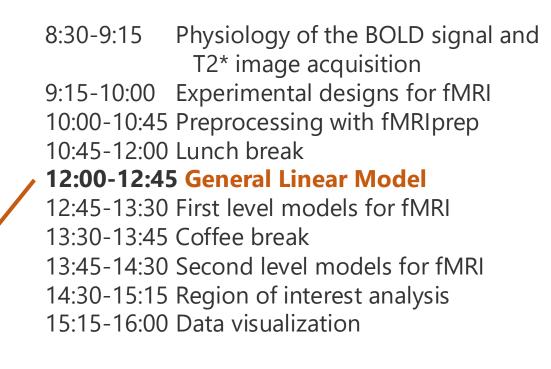
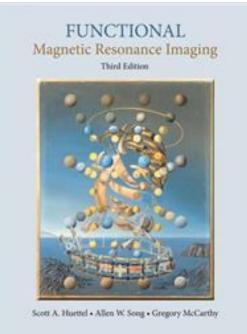
GLM for fMRI analysis

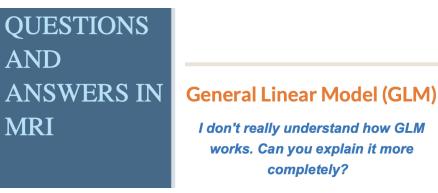
3.9.2024 Kerttu Seppälä PhD Student, Turku PET Centre kerttu.seppala@utu.fi







<u>Huettel Scott A.</u>, <u>Song Allen W.</u>, <u>McCarthy</u> <u>Gregory</u>: Functional Magnetic Resonance Imaging, 2014, <u>Oxford University Press Inc</u>



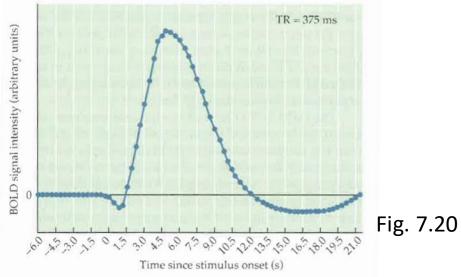
https://mriquestions.com/general-linear-model.html



http://www.newbi4fmri.com/tutorial-3-glm

Recap: The Actual Measured Signal Changes in BOLD activation after presenting single event stimuli for subject from a voxel Stimulus on Stimulus on Arbitary Units Notice also the delay after the stimulus and before the peak 100 50 75 25 Fig. 7.9 Time (s) Example of BOLD hemodynamic response to a hand squeezing task TR = 375 ms

Hand squeezing Fig. 7.12



FUNCTIONAL

Spatial Resolution

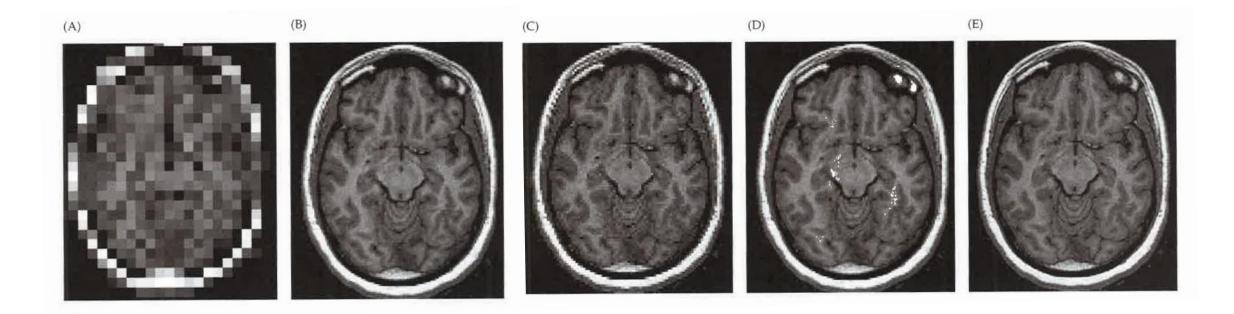
Spatial Resolution: Ability to

within an image

distinguish different locations



Figure 1.7 The human brain at different spatial resolutions. Spatial resolution refers to the ability to resolve small differences in an image. In general, we can define spatial resolution based on the size of the elements (i.e., voxels) used to construct the image. The images shown here present the same brain sampled at five different element sizes: 8 mm (A); 4 mm (B); 2 mm (C); 1.5 mm (D); and 1 mm (E). Note that the gray–white structure is well represented in the latter three images, all of which were produced using element sizes that were less than half the typical gray matter thickness of 5 mm.



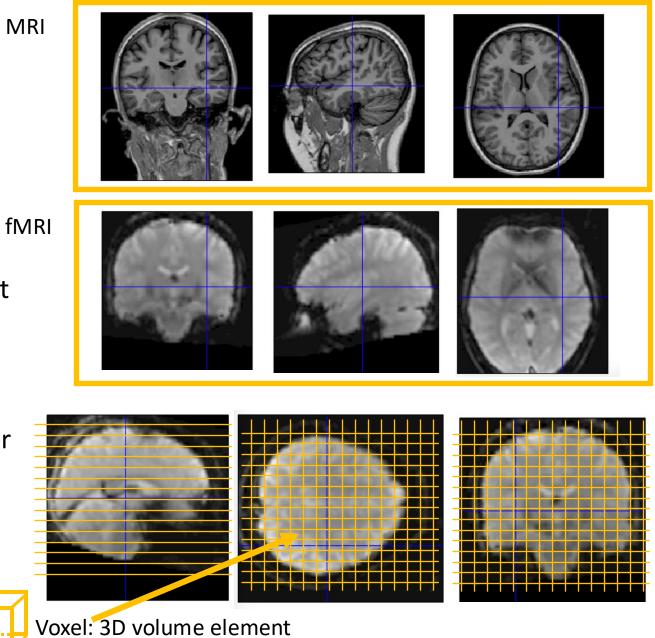
MRI

Spatial Resolution 2

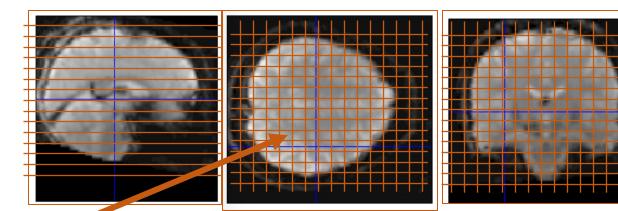
- Structural images voxels maybe $1 \times 1 \times 1 \text{ mm}$
- Functional images voxels maybe 3 x 3 x 3 mm (depends on the question)
- BOLD signal is direct measure of the amount of deoxyhemoglobin in a voxel
- Partial volume effects: combination of different tissue types within a voxel (effect from large arteries / small capillaries)
- \rightarrow Spatial smoothing for statistics and better signal-to-noise ratio

	Spatial Scales in the Human Brain	
Structure	Scale (mm)	
Brain	100	
Gyri	10	
Dominance co	lumn 1	

Structure	Scale (mm)	
Neuron	0.01	
Synapse	0.001	
Ion channel	0.00001	

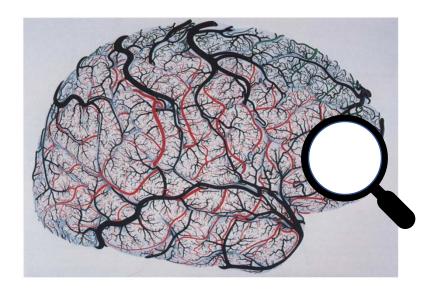


30 slices, 64 x 64 voxels per slice \rightarrow 122800 voxels





Partial volume effects



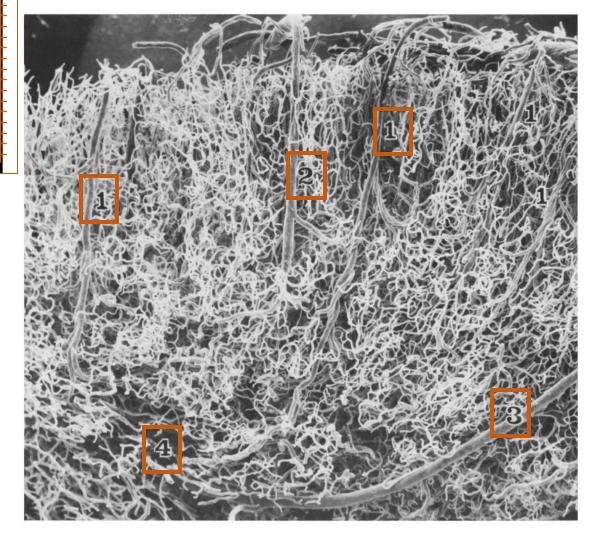


FIG. 60. Temporal pole (SEM). Male, 66 years. General view of the cortical vessels. (1) Cortical arteries. (2) Cortical vein. (3) Medullary artery (type A6). (4) Subcortical white matter (\times 40).

Duvernoy HM, Delon S, Vannson JL. Cortical blood vessels of the human brain. Brain Res Bull. 1981 Nov;7(5):519-79. doi: 10.1016/0361-9230(81)90007-1. PMID: 7317796.

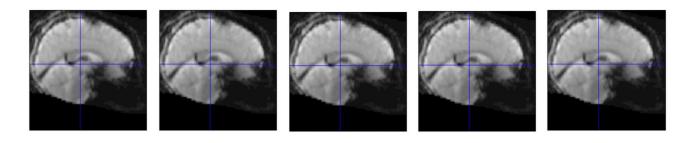
Temporal Resolution

- Determined by TR and by limitations of vascular system
 - TR = time of repetition (time for a volume)
 - HDR rises and falls within 10-15 s
 - Duration of the stimulus does not necessarily correspond with duration of neuronal activity
- sagittal axial coronal

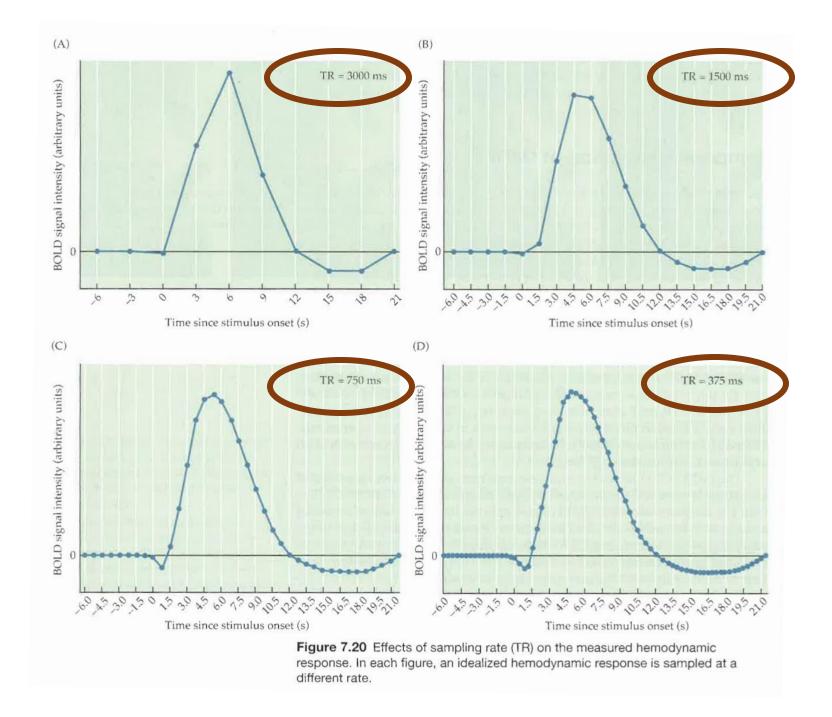
- fMRI is slow
 - neuronal activity is short < 1s
 - no snapshot of neuronal activity but an estimate of slower changes in vascular system
- Good TR?
 - Depending on the experiment (0,5 s 3 s)
 - Smaller TR

 \rightarrow more accurate estimation of HDR shape; not necessary effect on amplitude One volume, takes TR to collect

30 slices, 64 x 64 voxels per slice \rightarrow 122800 voxels

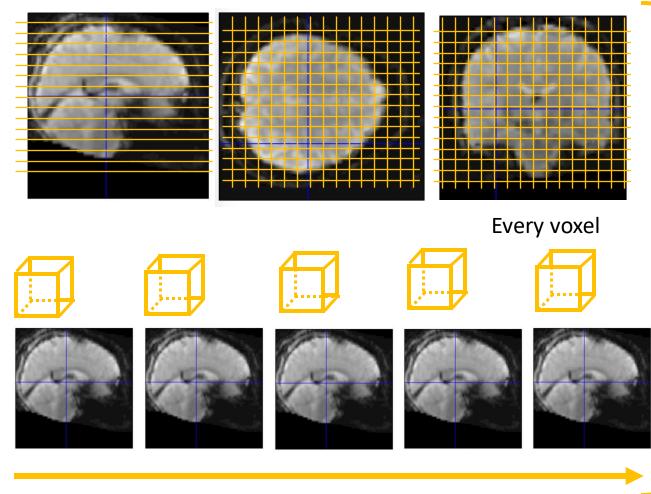


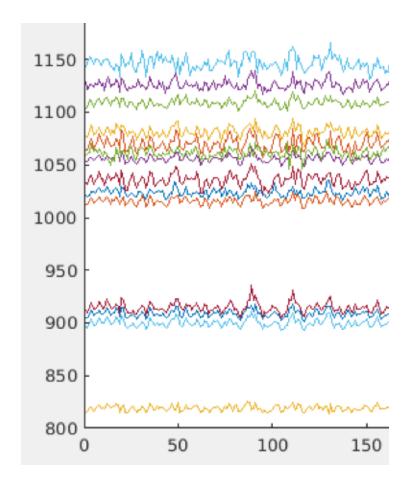
Many volumes over time





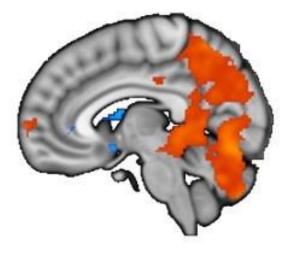
Timeseries



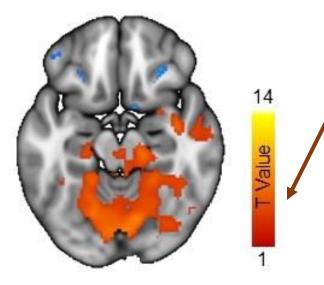


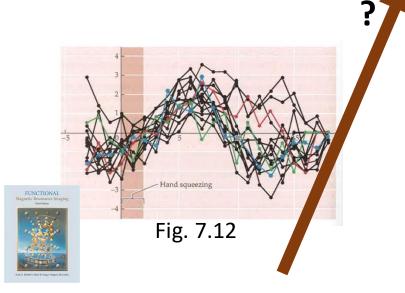
Many volumes over time

Conjuring 2









Supplementary Figure 2. The relationship between experienced fear and neural activity for Conjuring 2.

Fear ratings were convolved with a hemodynamic response function and entered as a regressor into a GLM analysis with a high-pass filter of 256s (uncorrected p = 0.001).

Hudson et al. "Dissociable neural systems for unconditioned acute and sustained fear", NeuroImage, Vol 216, 2020.

Linearity of the Hemodynamic Response



Linear system

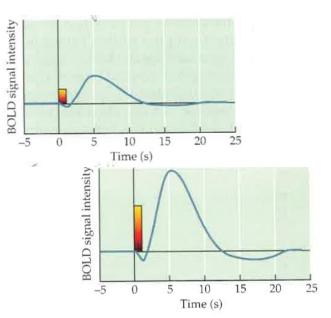
- System: for a given input the system will respond with the same output
- Input: neuronal activity is a short-duration input
- Output: HDR
- Principles of linear system 1) Scaling + 2) Superposition

1) Scaling

- The magnitude (amplitude) of the system output must be proportional to the system input
- Test condition and control condition:
 - neuronal activity in task required twice as much of work as in rest condition, so the amplitude of HDR is more in activation than in rest
 - if no interference, the brain areas are not activating so

2) Superposition

- Total response to a set of imputes is equivalent to the summation of the independent responses to the inputs
- 1 event creates 1 HDR, 2 events create combined response equal to two individual responses added together



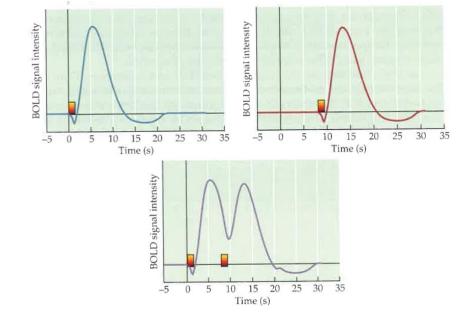




Fig 7.28



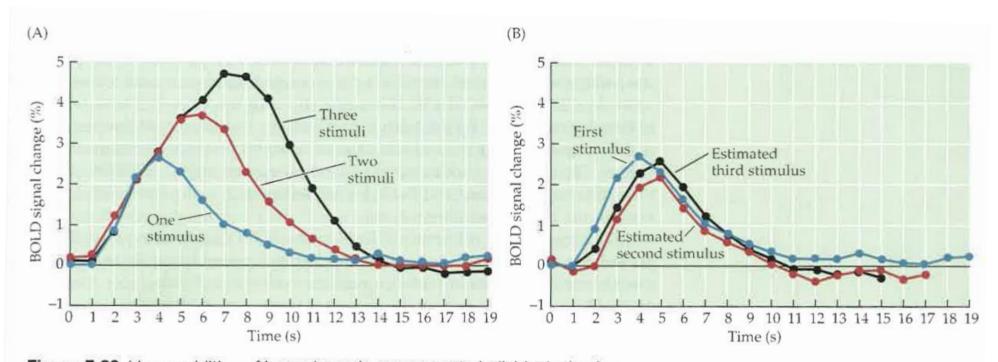


Figure 7.29 Linear addition of hemodynamic responses to individual stimulus events. (A) The hemodynamic responses evoked by presentation of one, two, or three identical stimuli (short-duration visual flashes) at short interstimulus intervals were measured. Shown here are data from a 2-s interval. The total hemodynamic response increased in a regular fashion as the number of stimuli in a trial increased. (B) By subtracting the one-stimulus trial from the two-stimulus trial and subtracting the two-stimulus trial from the three-stimulus trial, the contributions of the second and third stimuli in a trial were estimated. The responses to the second and third stimuli were generally similar to the response to the first stimulus, suggesting that the BOLD response scales in a roughly linear fashion. (From Dale and Buckner, 1997.)

Limitations in Linearity of HDR



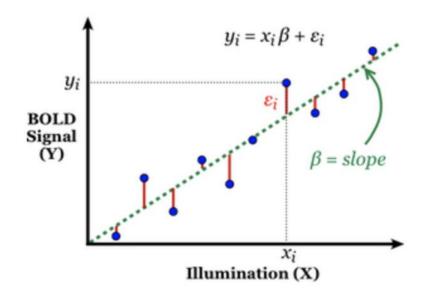
- Limitation: short stimuli intervals create more deviation in HDR \rightarrow less linear system, BUT more data and more statistical power
- Limitation coming from refractory period: a time period following the presentation of a stimulus during which subsequent stimuli evoke a reduced response, around 6 s
- \rightarrow refractory period differs between the brain areas
- → However, offers possibility for further studies in brain science, but requires advanced modelling

GLM for fMRI

General Linear Model



• Because the system is linear, the modelling can be linear



Simplified linear regression example, adapted from data of Hansen et al (2004)

http://mriquestions.com/general-linear-model.html

$$y = \beta X + \varepsilon$$

- Y = measured signal (BOLD)
- **X** = the stimuli for the subject

Because the system is linear, we hope that modelling it as such will explain the brain activity found, so:

B = find the best ones that leaves the error minimizedE = error

So: 1) create a model, 2) fit the model with the data and 3) do the statistical tests \rightarrow beautiful activation maps and pictures



$$y_{1} = x_{1}\beta + \varepsilon_{1}$$

$$y_{2} = x_{2}\beta + \varepsilon_{2}$$

$$y_{3} = x_{3}\beta + \varepsilon_{3}$$

$$\vdots$$

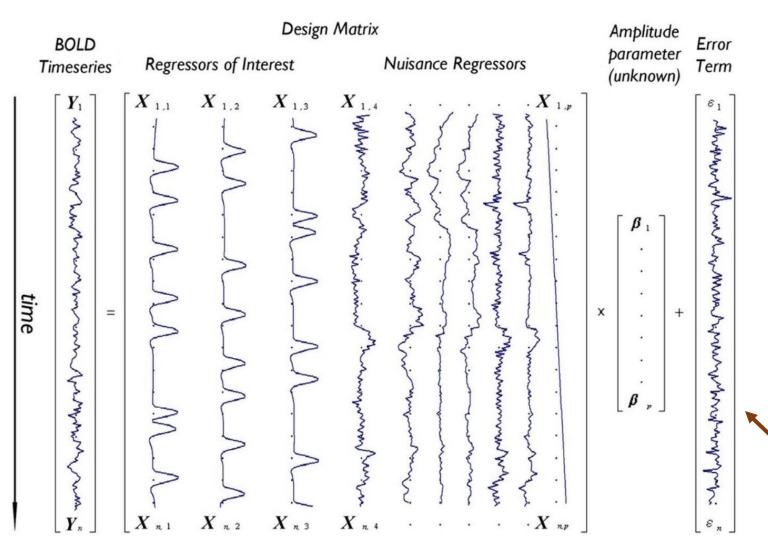
$$y_{n} = x_{n}\beta + \varepsilon_{n}$$

$$\begin{bmatrix}y_{1}\\y_{2}\\y_{3}\\\vdots\\y_{n}\end{bmatrix} = \begin{bmatrix}x_{1}\\x_{2}\\x_{3}\\\vdots\\x_{n}\end{bmatrix} \begin{bmatrix}\beta\end{bmatrix} + \begin{bmatrix}\varepsilon_{1}\\\varepsilon_{2}\\\varepsilon_{3}\\\vdots\\\varepsilon_{n}\end{bmatrix}$$

$$\longrightarrow$$

$$\mathbf{Y} = \mathbf{X}\beta + \varepsilon$$

Y and $\boldsymbol{\varepsilon}$ a single voxel at successive time points (*i* = 1 to *n*).



Depiction of the General Linear Model (GLM) for a voxel with time-series **Y** predicted by a design matrix **X** including 10 effects (three regressors of interest – e.g., tasks A,B,C – and seven nuisance regressors – e.g., six motion parameters and one linear drift). Calculated weighting factors ($\beta_1 - \beta_{10}$) corresponding to each regressor are placed in amplitude vector **B** while column vector **c** contains calculated error terms (ϵ_i) for the model corresponding to each time point *i*. (From Monti, 2011, under CC BY license)

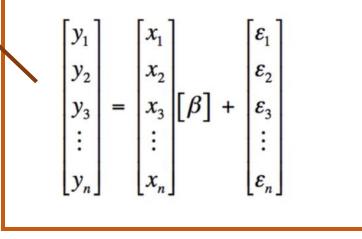
"Stated in words, the GLM says that **Y** (the measured fMRI signal from a single voxel as a function of time) can be expressed as the sum of one or more experimental design variables (**X**), each multiplied by a weighting factor ($\boldsymbol{\beta}$), plus random error ($\boldsymbol{\epsilon}$)"

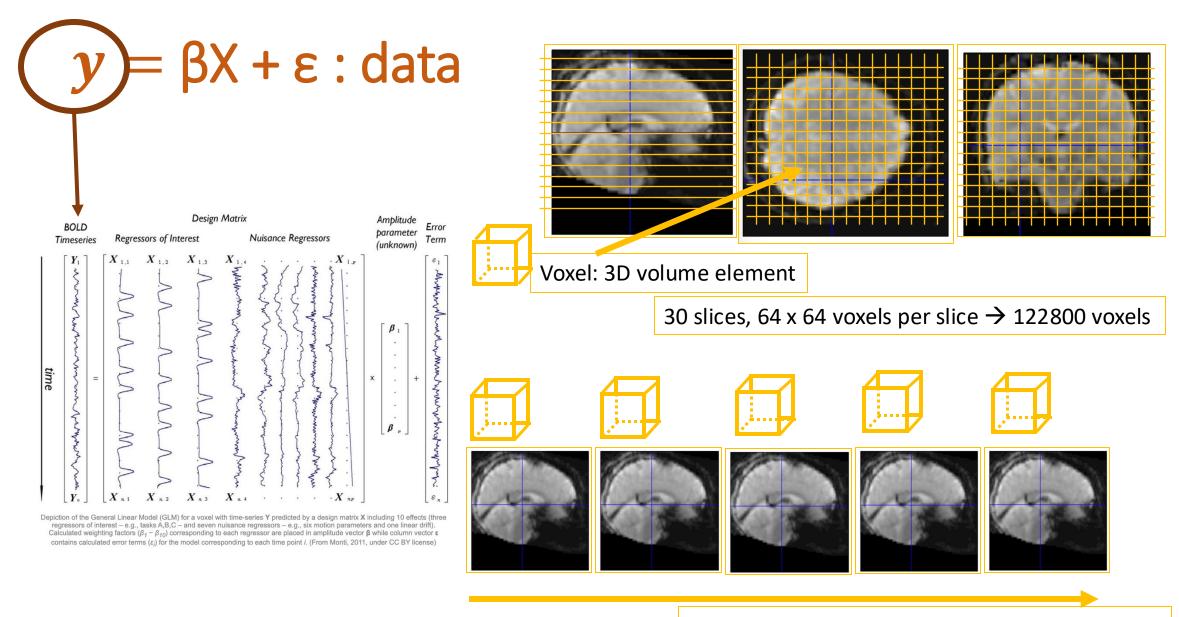
ANSWERS IN General Linear Model (GLM

I don't really understand how GLM works. Can you explain it more

MRI

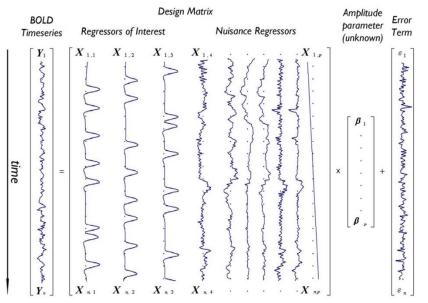
http://mriquestions.com/general -linear-model.html





The same voxel imaged at each TR \rightarrow Timeserie





Depiction of the General Linear Model (GLM) for a voxel with time-series Y predicted by a design matrix X including 10 effects (three regressors of interest – e.g., tasks A,B,C – and seven nuisance regressors – e.g., six motion parameters and one linear drift). Calculated weighting factors ($\beta_1 - \beta_{10}$) corresponding to each regressor are placed in amplitude vector β while column vector ϵ contains calculated error terms (ϵ_j) for the model corresponding to each time point *i*. (From Monti, 2011, under CC BY license)

<u>Essential</u> regressors

- Expectation shape of the *HRF*, if a voxel of interest gets activated during to a stimulus
- Time runs from top to down
- Must be independent from each others (can't explain the same variance)

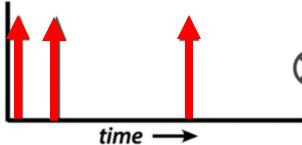
Nuisance regressors

- Factors that confound the analysis but not interesting by themselves
 - Head movement
 - Scanner drifts
 - Physiological signals (heart)
- Helps with the GLM:
 - Reduce the amount of error
 - Improves validity of the GLM (model assumes the residuals being independend and identically distributed as Gaussian noise)

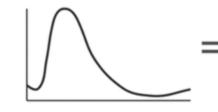


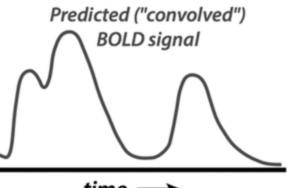


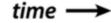
Events/stimuli



Hemodynamic Response Function (HRF)

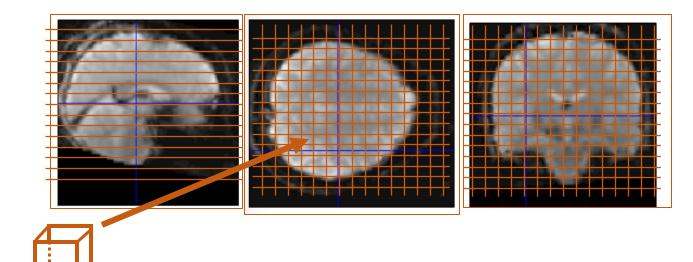


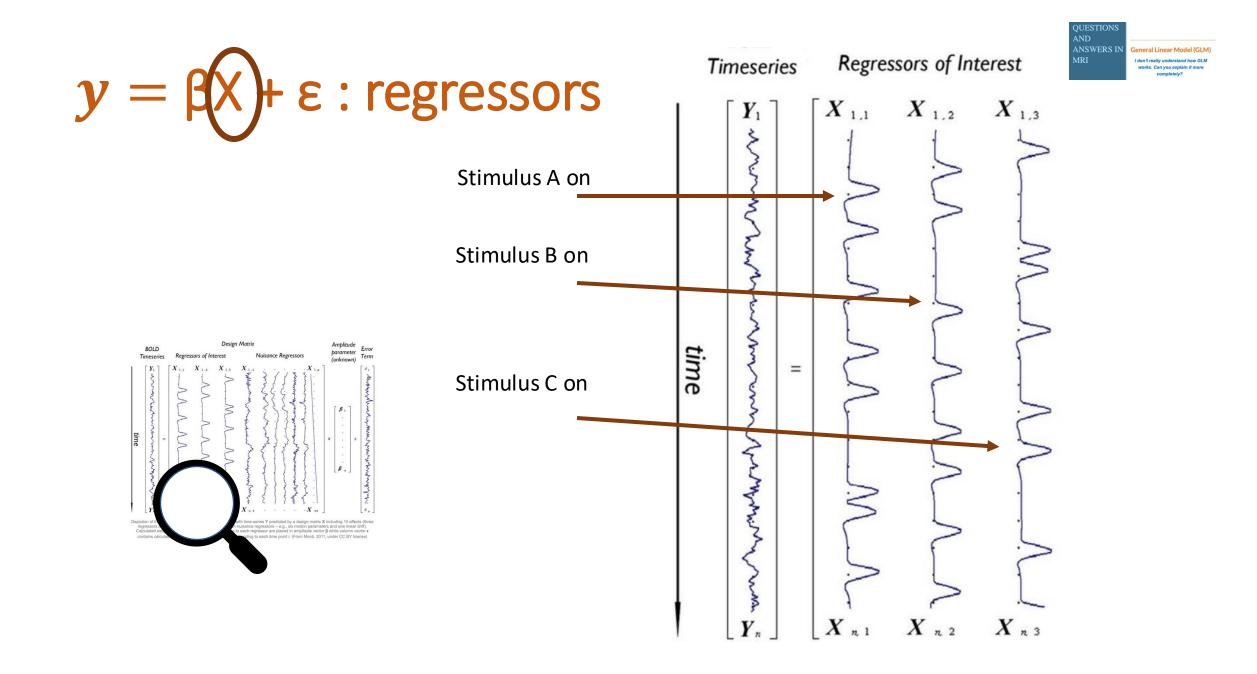


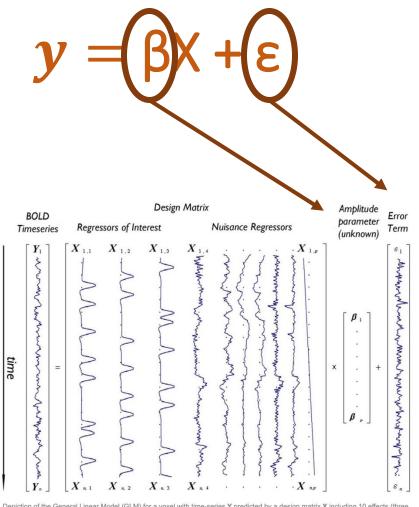


Simuli A (bright light) B (medium bright light) C (not bright light)

Red arrows above points timing for A
 → Might find a voxel showing HRF as illustrated in the visual cortex







Depiction of the General Linear Model (GLM) for a voxel with time-series Y predicted by a design matrix X including 10 effects (three regressors of interest – e.g., tasks A,B,C – and seven nuisance regressors – e.g., six motion parameters and one linear drift). Calculated weighting factors ($\beta_1 - \beta_{10}$) corresponding to each regressor are placed in amplitude vector β while column vector ϵ contains calculated error terms (ϵ_i) for the model corresponding to each time point *i*. (From Monti, 2011, under CC BY license)

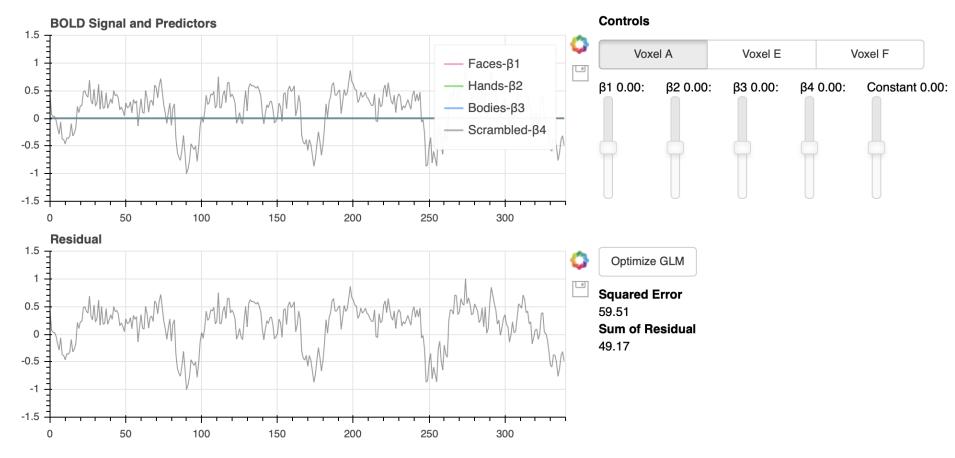
- $\boldsymbol{\varepsilon} = \text{error}$
- Aim to be mimized (patient trainingn, scanner optimization, preprocessing, modeling....)

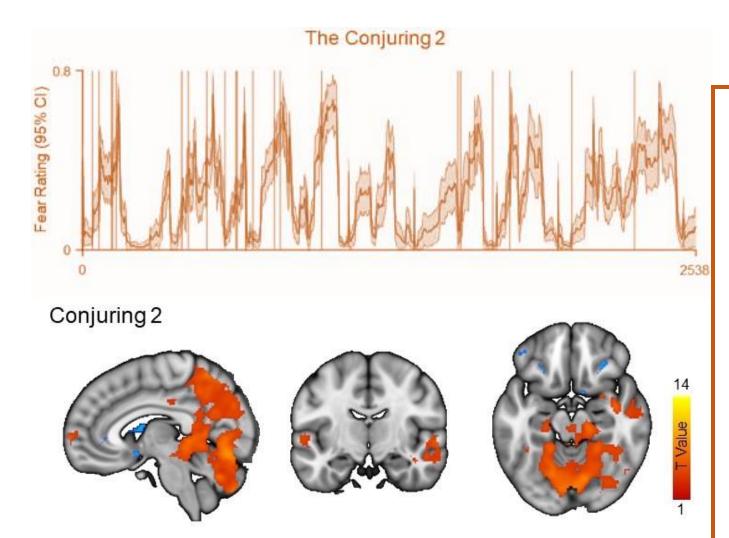
- β and ϵ vectors are computed
- \rightarrow Statistical testing for hypothesis
- Statistical Parametric Map
 (SPM) or Posterior Probability Map (PPM)



http://129.100.119.110:22028/GLM-LocalizerPred

http://www.newbi4fmri.com/tutorial-3-glm





Supplementary Figure 2. The relationship between experienced fear and neural activity for Conjuring 2.

Fear ratings were convolved with a hemodynamic response function and entered as a regressor into a GLM analysis with a high-pass filter of 256s (uncorrected p =0.001).

Hudson et al. "Dissociable neural systems for unconditioned acute and sustained fear", NeuroImage, Vol 216, 2020.

Limitations and Assumptions



- Hemodynamic response might differ across the brain areas but the model is the same for each voxel (betas calculated separately)
- Model assumes that noise varies with a normal distribution in each voxel in each time point (differs greatly close to large arteries)
- Model assumes also independent statistical test for each voxel (adjacent voxels have similar properties)

Summary

- Linear System: for a given input the system will respond with the same output
- GLM: General linear model

$$y = \beta X + \varepsilon$$

"Stated in words, the GLM says that Y (the measured fMRI signal from a single voxel as a function of time) can be expressed as the sum of one or more experimental design variables (X), each multiplied by a weighting factor (β), plus random error (ε)"

[http://mriquestions.com/general-linear-model.html]

Question Time!